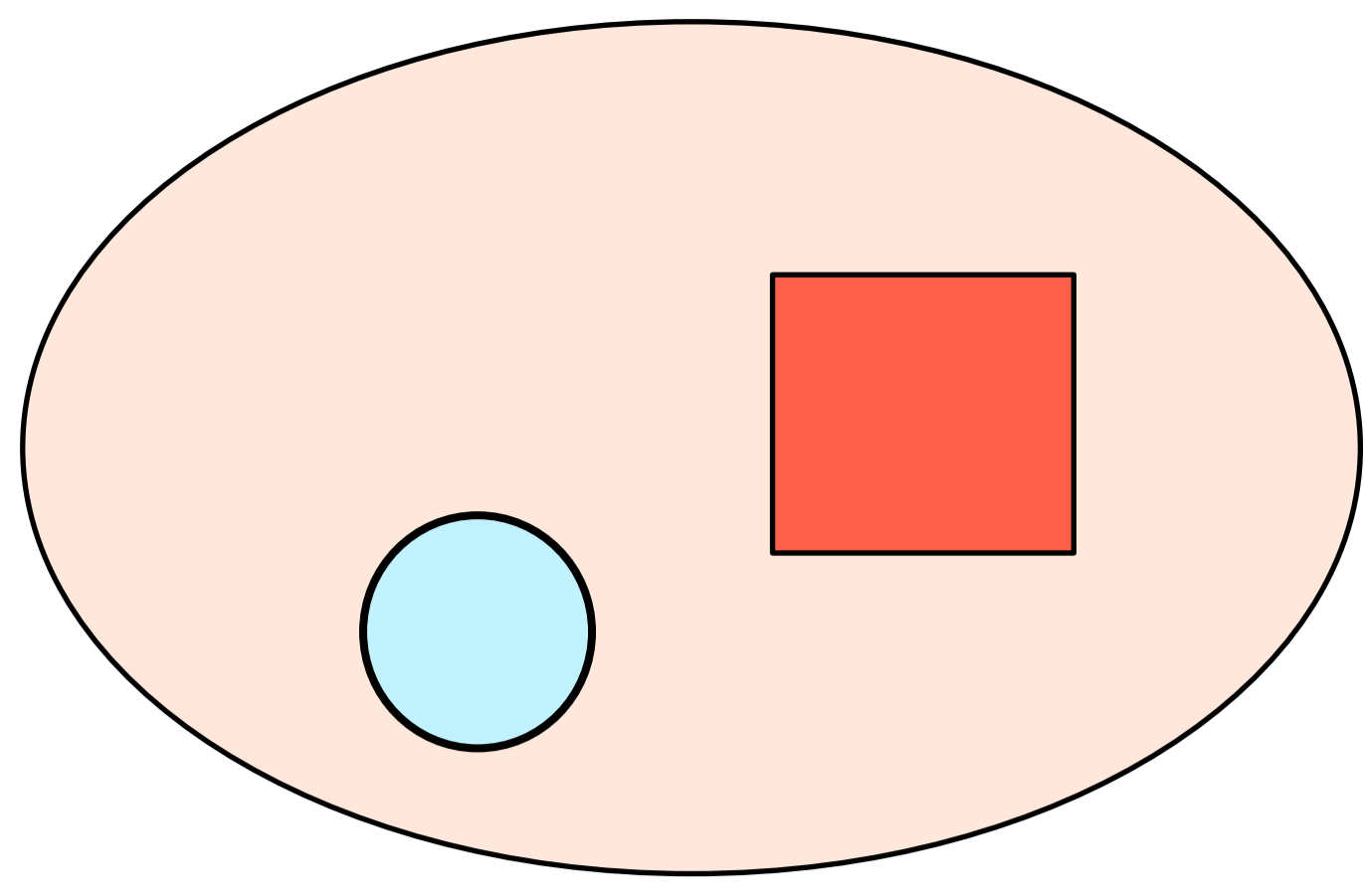
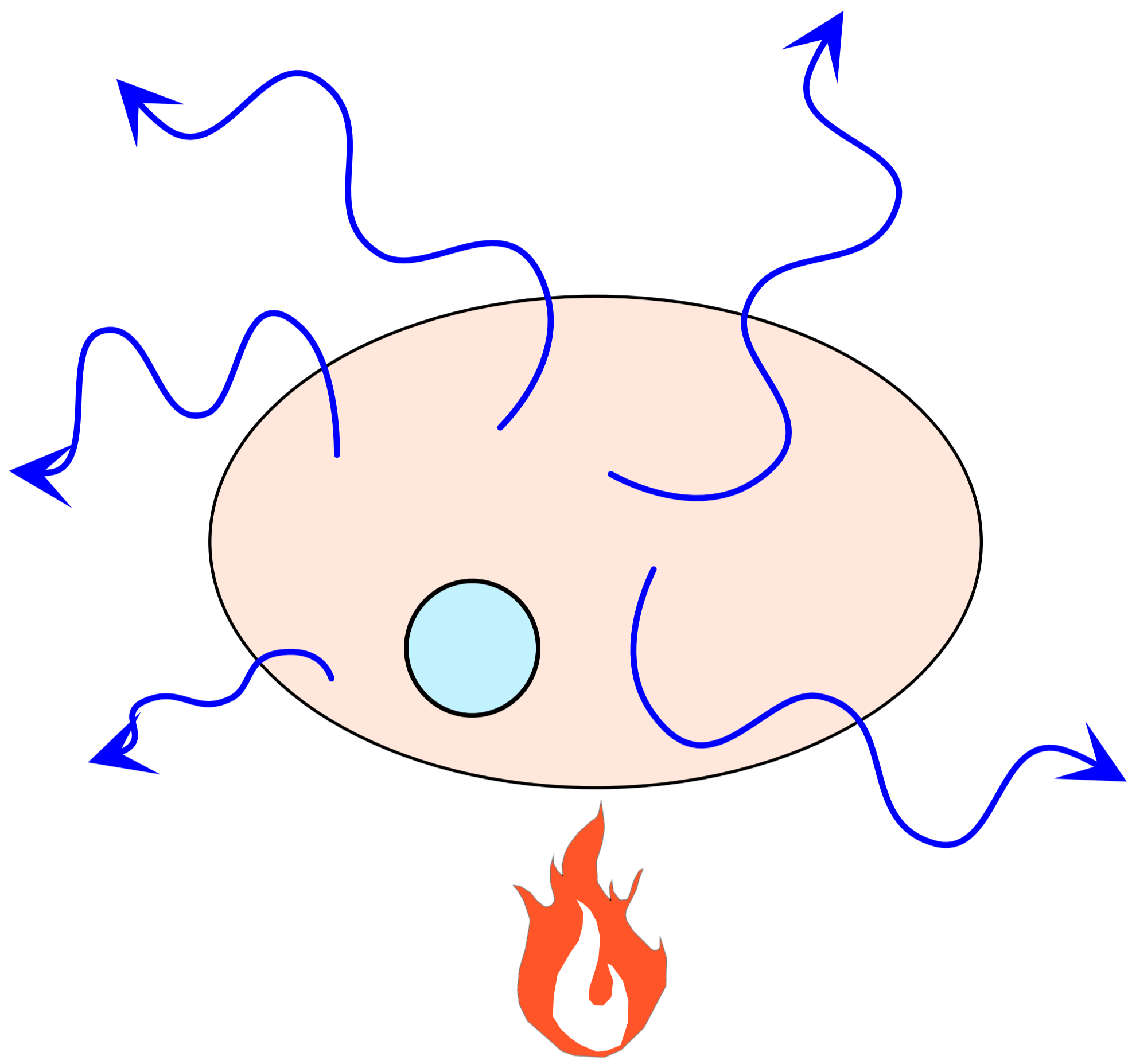


# H<sub>2</sub>O restoration

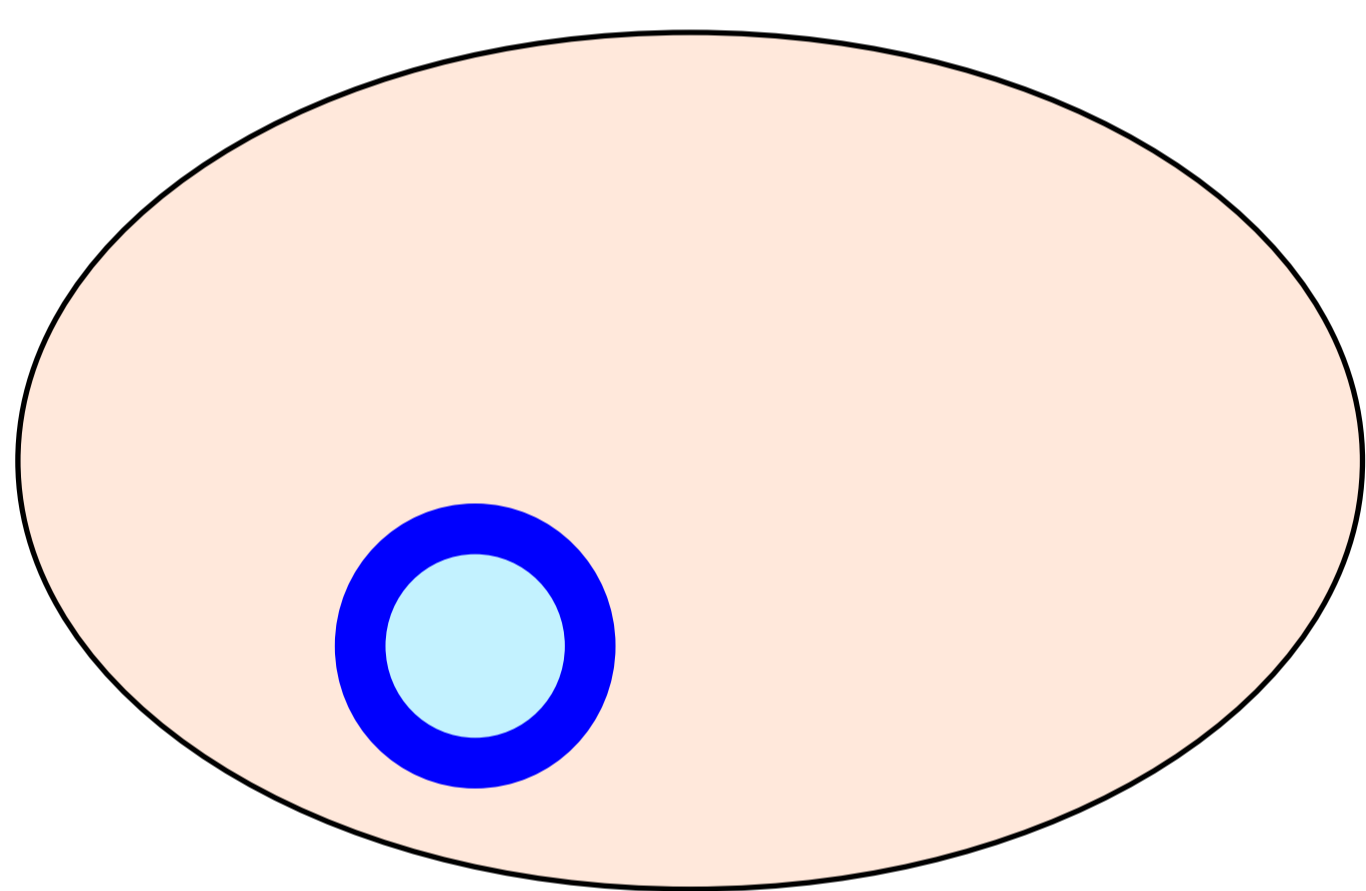
The starting H<sub>2</sub>O contents of the MI studied to be corrected is the H<sub>2</sub>O concentration of the glass. The the H<sub>2</sub>O concentration of the glass was based on SIMS analysis.



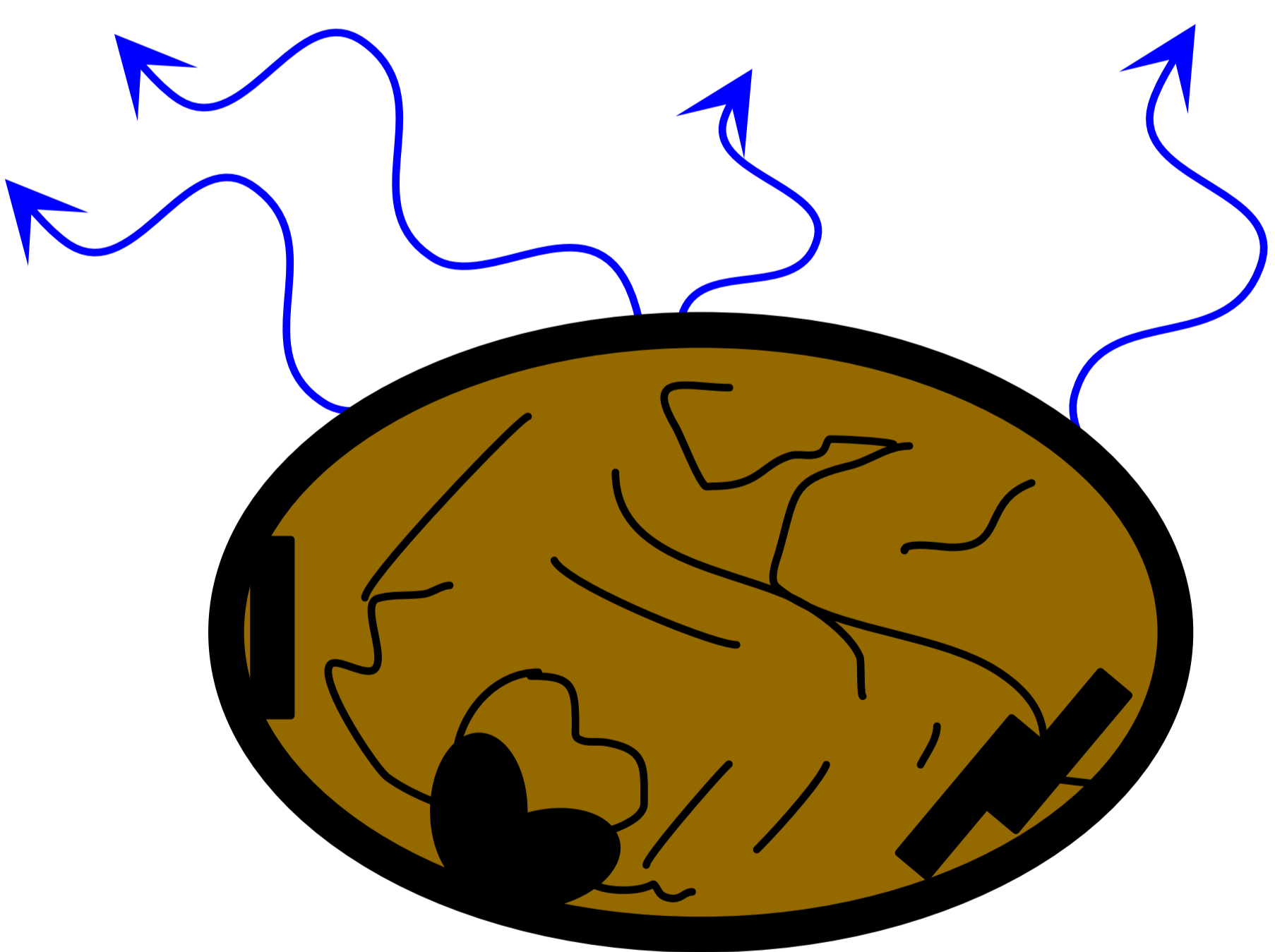
*Step I: SIMS analysis of glasses of MI*



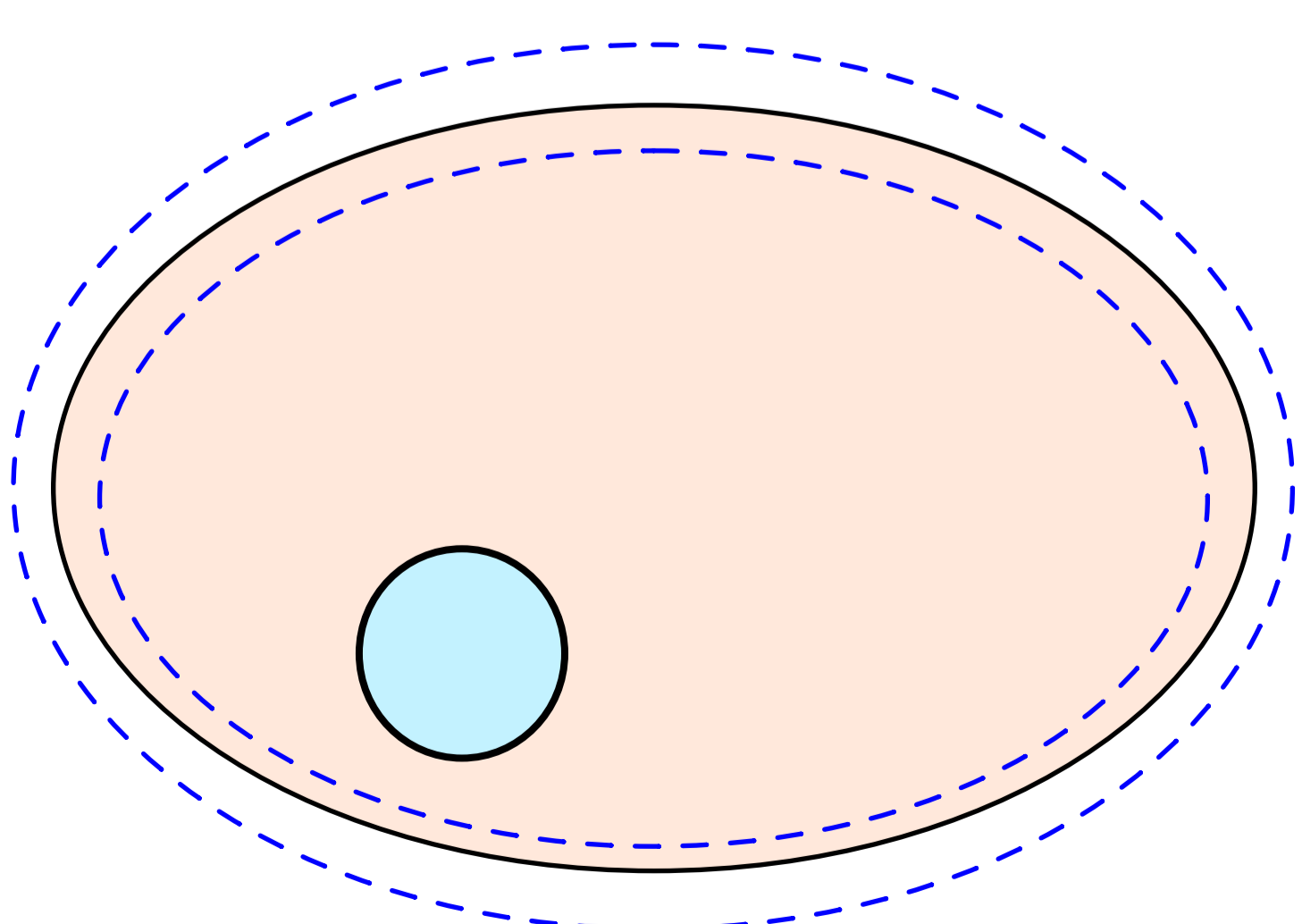
*Step II: addition of H<sub>2</sub>O lost by heating experiments*



*Step III: addition of H<sub>2</sub>O contained in the bubble*



*Step IV: addition of H<sub>2</sub>O lost by post-eruption cooling*



*Step V: addition-subtraction of H<sub>2</sub>O by PEC*

+

H<sub>2</sub>O-loss during heating experiments. This correction is applied to all MI studied. H<sub>2</sub>O loss estimated based on Eq. 12 by Qin et al. (1992). We provided a visual basic code in Appendix file A7 to calculate H<sub>2</sub>O loss based on coefficient, D, radius of MI and its host, and densities of melt and host.

+

H<sub>2</sub>O content loss into the bubble lining as liquid H<sub>2</sub>O. This correction is based on Raman signals of liquid H<sub>2</sub>O or gypsum reported by Esposito et al. (2016), and based on the composition of the fluid estimated using MafiCH solubility model and the composition of the glass of the bubble-bearing MI. This correction is applied to all bubble-bearing MI.

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H<sub>2</sub>O-loss during natural post eruption cooling of lavas. Correction applied only to the 5 MI hosted in olivine from lavas (sample Somma Caldera >33 ka). H<sub>2</sub>O-loss is calculated based on the comparison between MI hosted in olivine from lava with those hosted in olivine from pumice lapilli.

±

H<sub>2</sub>O adjustment based on estimated PEC. This correction is applied to all MI studied. When PEC is positive (olivine added back to the melt), the H<sub>2</sub>O is subtracted to the H<sub>2</sub>O of the melt calculated after the previous steps. When the PEC is negative (olivine subtracted from the melt), the H<sub>2</sub>O is added to the H<sub>2</sub>O of the melt calculated after the previous steps.